Prof. Dr. Alfred Toth

# Raumsemiotik mit trajektischen Abbildungen

1. In Toth (2025) hatten wir das vollständige System der $3^3 = 27$ ternären (triadisch-trichotomischen) semiotischen Relationen in Form von trajektischen Abbildungen der Form

$$T = (1, 2, 3) \mid (1, 2, 3) \text{ mit } \mid = R((1, 2, 3), (1, 2, 3))$$

dargestellt und und die semiotischen Relationen nach dem Vorschlag Walthers für Zeichenklassen (vgl. Walther 1979, S. 79) in Kompositionen dyadischer Teilrelationen zerlegt

$$(3.x, 2.y, 1.z) = (3.x \rightarrow 2.y) \circ (2.y \rightarrow 1.z)$$

$$(z.1, y.2, x.3) = (z.1 \rightarrow y.2) \circ (y.2 \rightarrow x.3).$$

2. In der vorliegenden Arbeit benutzen wir die trajektische Abbildungstheorie als algebraische Grundlage der von Bense inaugurierten Raumsemiotik (vgl. Bense/Walther 1973, S. 80). Die raumsemiotische Relation ist definiert durch

$$RR = (2.1, 2.2, 2.3) \times DRR = (3.2, 2.2, 1.2),$$

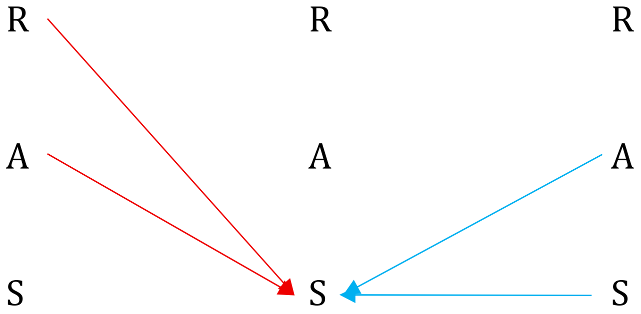
d.h. sie umfaßt die vollständige Primzeichenrelation P = (1, 2, 3) (vgl. Bense 1980). Im folgenden benützen wir folgende Buchstabenkürzel:

(2.1) := S(ystem), (2.2) := A(bbildung), (2.3) := R(epertoire)

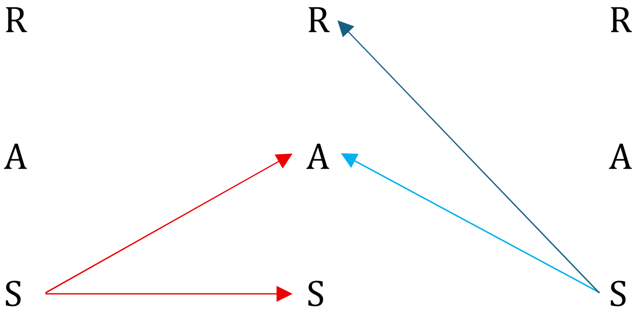
2. Raumsemiotische Relationen

1. Raumsemiotische Relation

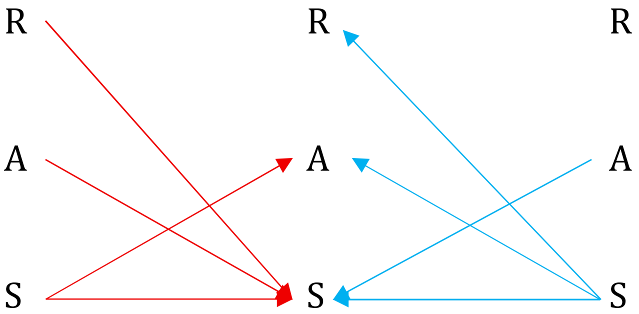
RR = (R.S, A.S, S.S)



DRR = (S.S, S.A, S.R)

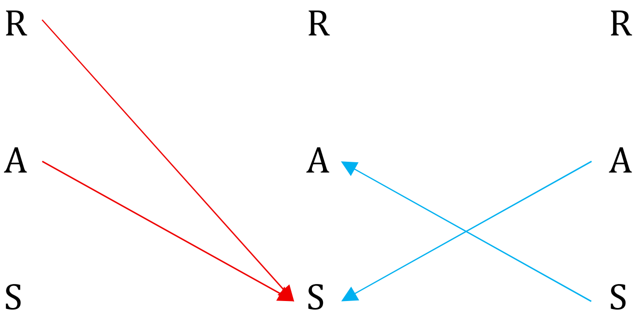



DS = [(R.S, A.S, S.S) × (S.S, S.A, S.R)]

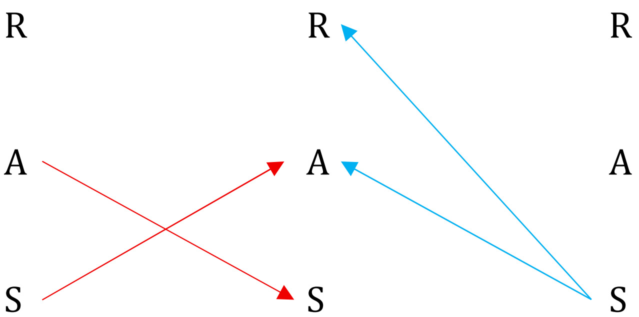



2. Raumsemiotische Relation

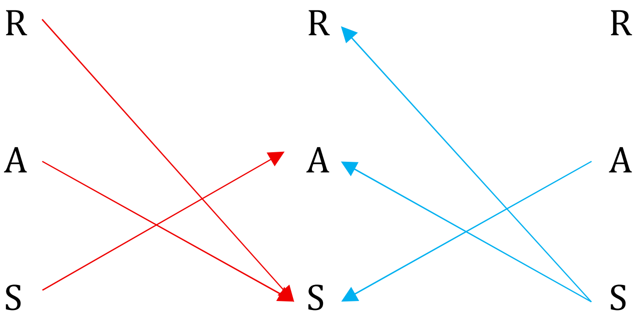
RR = (R.S, A.S, S.A)




DRR = (A.S, S.A, S.R)

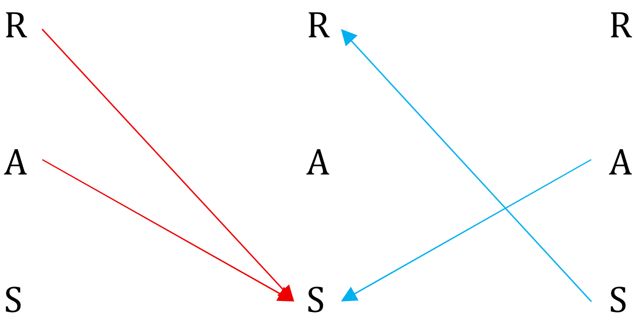


DS = [(R.S, A.S, S.A) × (A.S, S.A, S.R)]

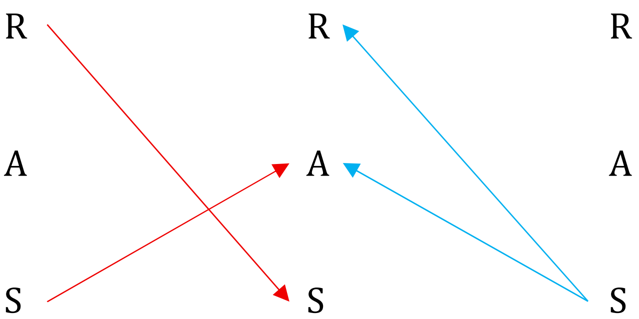



3. Raumsemiotische Relation

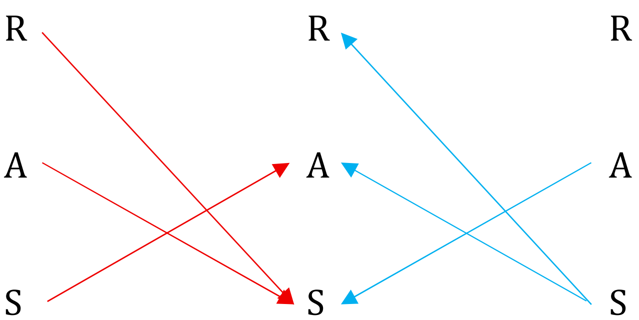
RR = (R.S, A.S, S.R)




DRR = (R.S, S.A, S.R)

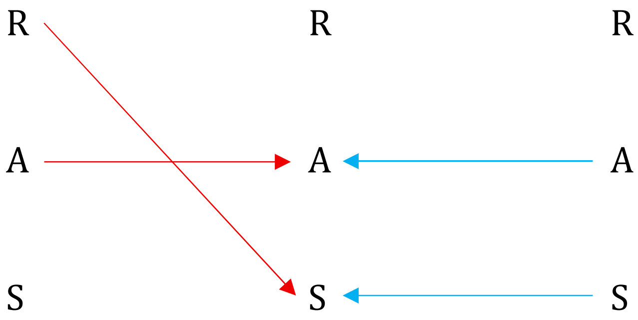



DS = [(R.S, A.S, S.R) × (R.S, S.A, S.R)]

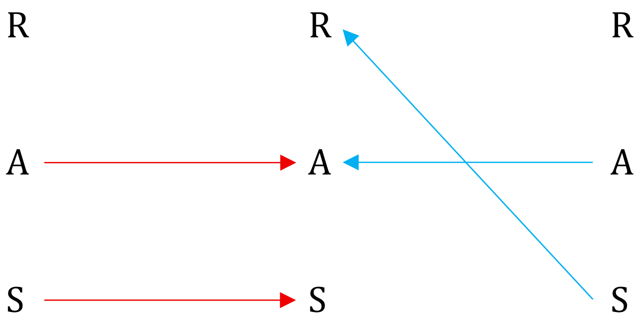


## 4. Raumsemiotische Relation

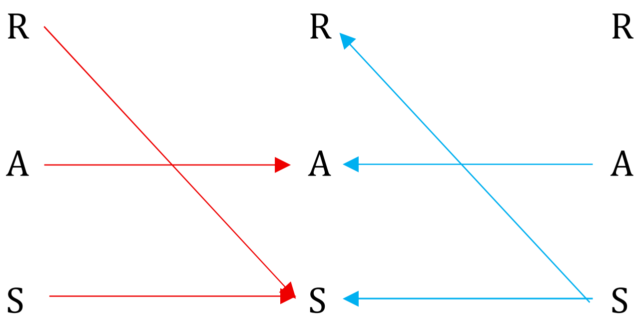
RR = (R.S, A.A, S.S)




DRR = (S.S, A.A, S.R)

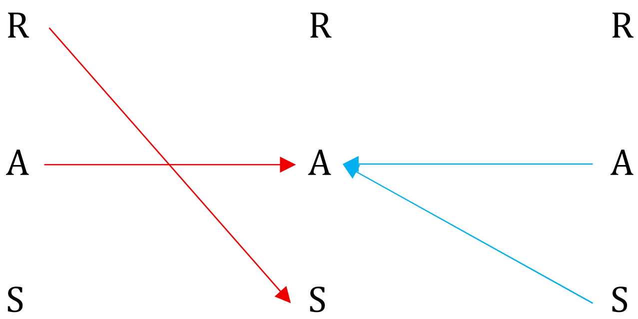



DS = [(R.S, A.A, S.S) × (S.S, A.A, S.R)]

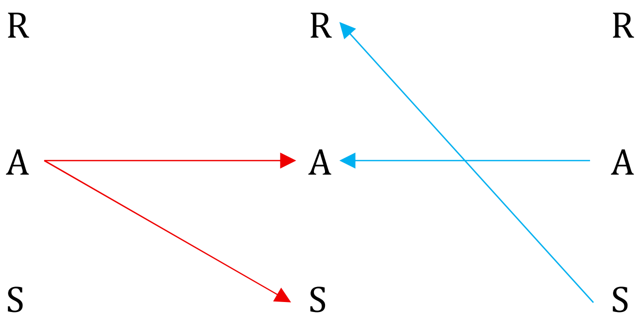



## 5. Raumsemiotische Relation

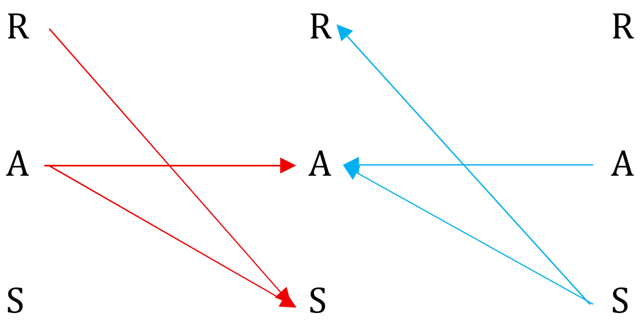
RR = (R.S, A.A, S.A)



DRR = (A.S, A.A, S.R)

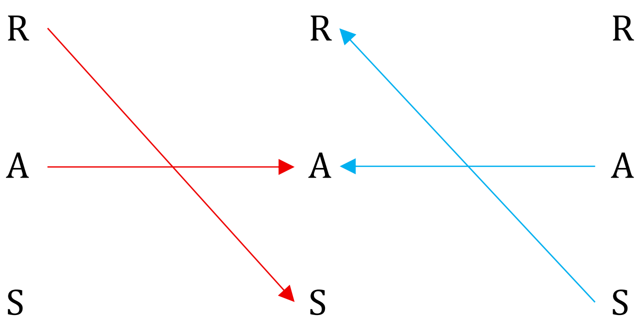



DS = [(R.S, A.A, S.A) × (A.S, A.A, S.R)]

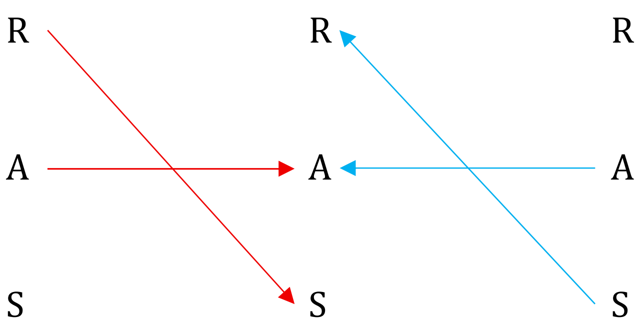



## 6. Raumsemiotische Relation

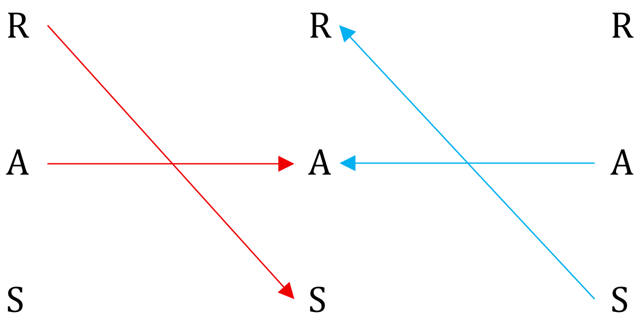
RR = (R.S, A.A, S.R)




DRR = (R.S, A.A, S.R)

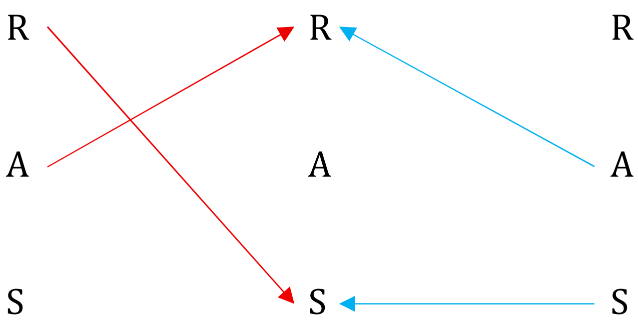


DS = [(R.S, A.A, S.R) × (R.S, A.A, S.R)]

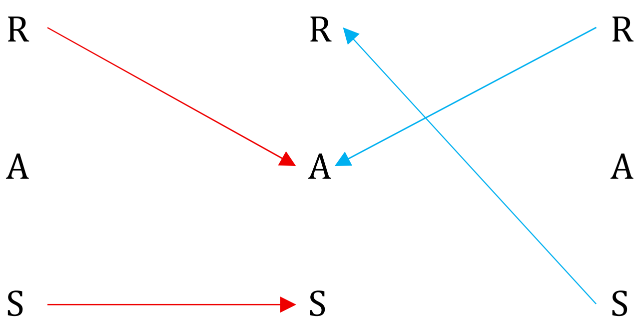



7. Raumsemiotische Relation

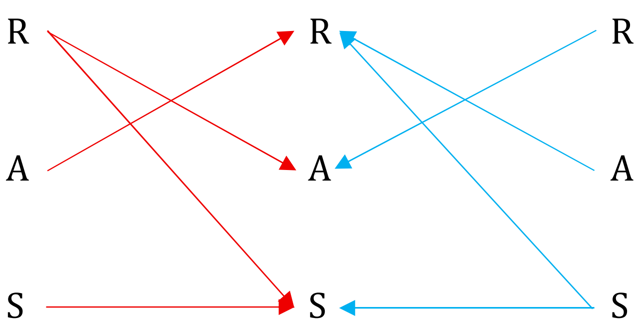
RR = (R.S, A.R, S.S)




DRR = (S.S, R.A, S.R)

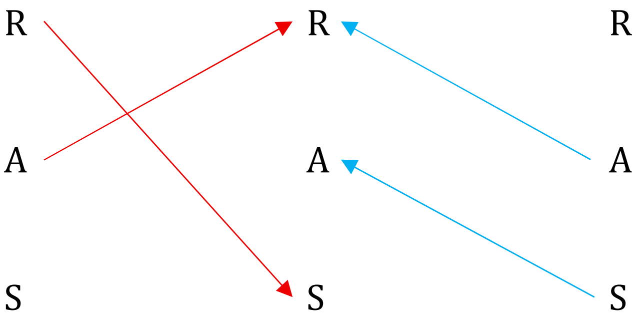



DS = [(R.S, A.R, S.S) × (S.S, R.A, S.R)]

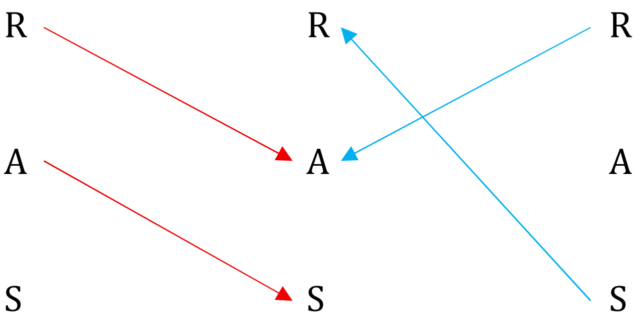


8. Raumsemiotische Relation

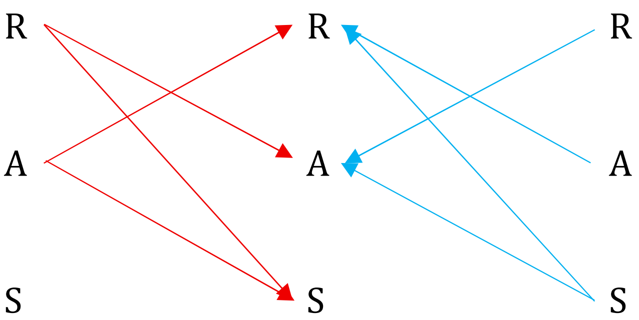
RR = (R.S, A.R, S.A)




DRR = (A.S, R.A, S.R)

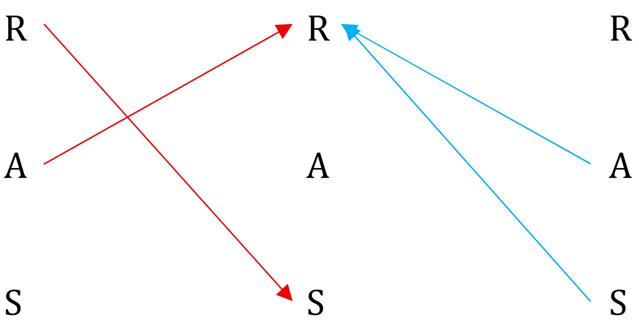



DS = [(R.S, A.R, S.A) × (A.S, R.A, S.R)]

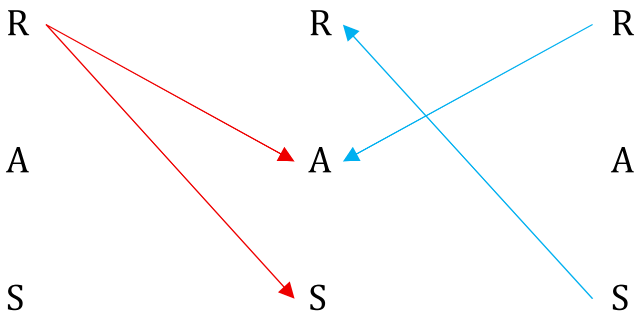



9. Raumsemiotische Relation

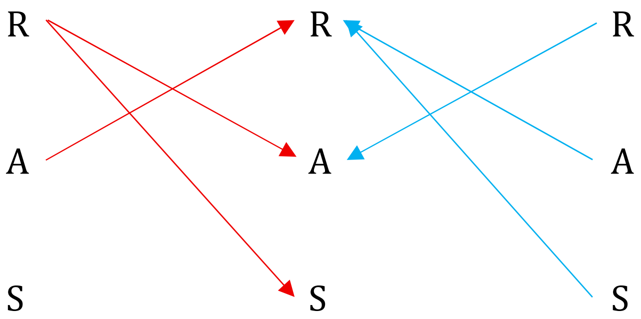
RR = (R.S, A.R, S.R)



DRR = (R.S, R.A, S.R)

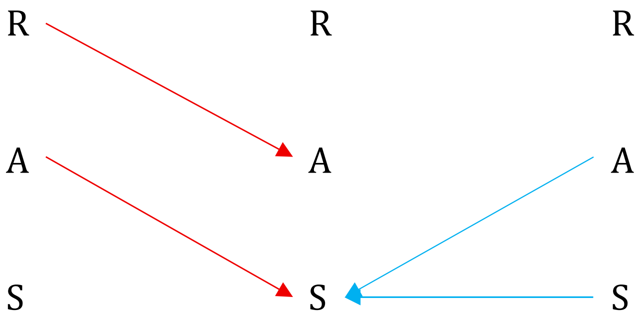



DS = [(R.S, A.R, S.R) × (R.S, R.A, S.R)]

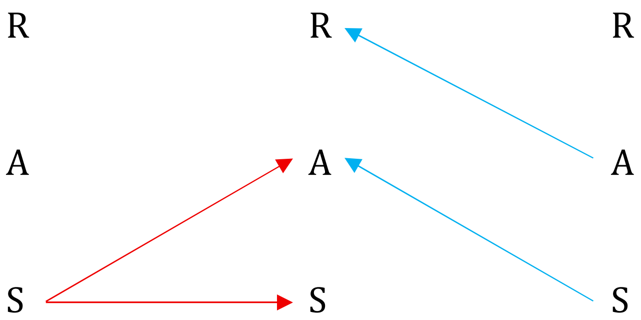



## 10. Raumsemiotische Relation

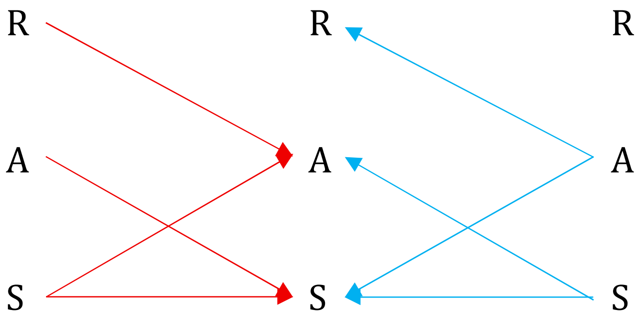
RR = (R.A, A.S, S.S)




DRR = (S.S, S.A, A.R)

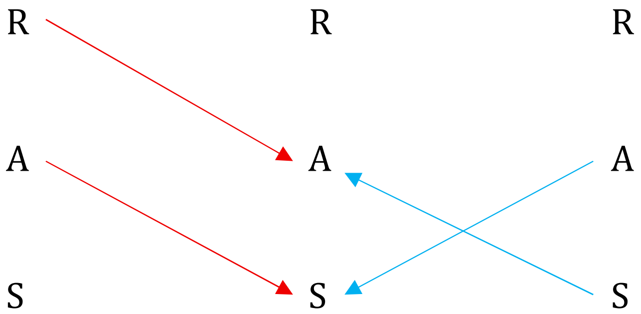


DS = [(R.A, A.S, S.S) × (S.S, S.A, A.R)]

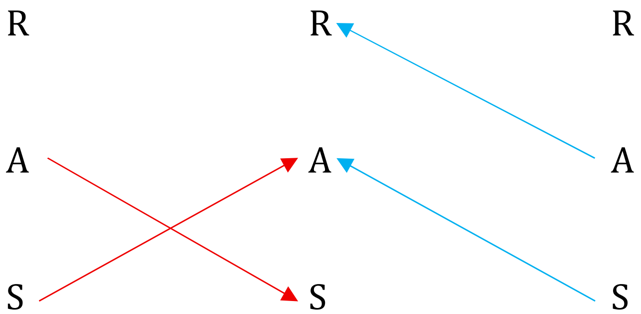



11. Raumsemiotische Relation

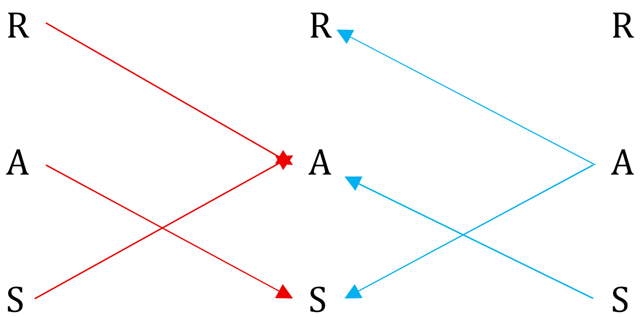
RR = (R.A, A.S, S.A)




DRR = (A.S, S.A, A.R)

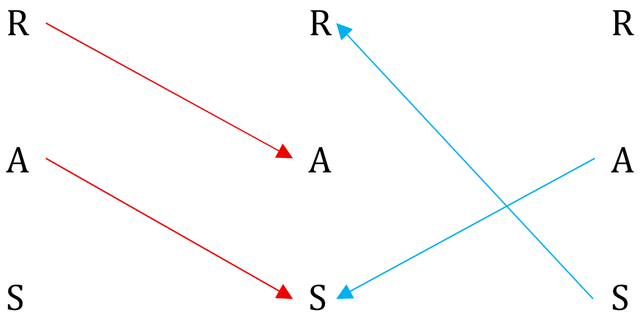



DS = [(R.A, A.S, S.A) × (A.S, S.A, A.R)]

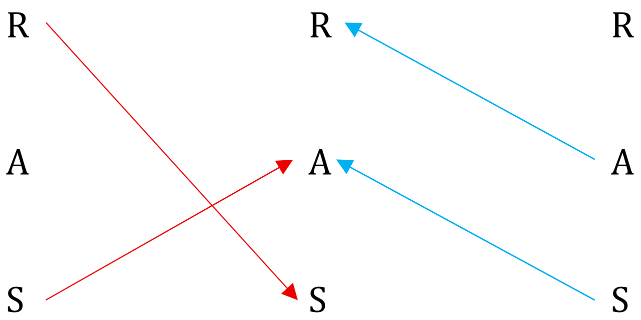


12. Raumsemiotische Relation

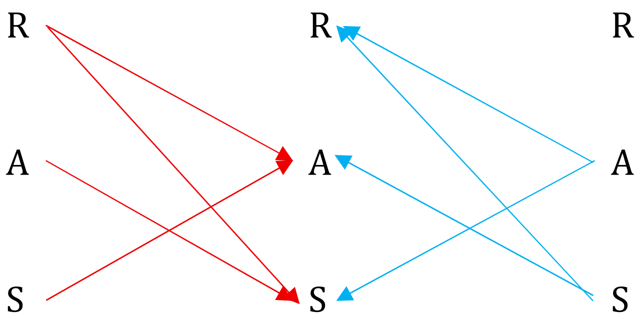
RR = (R.A, A.S, S.R)




DRR = (R.S, S.A, A.R)

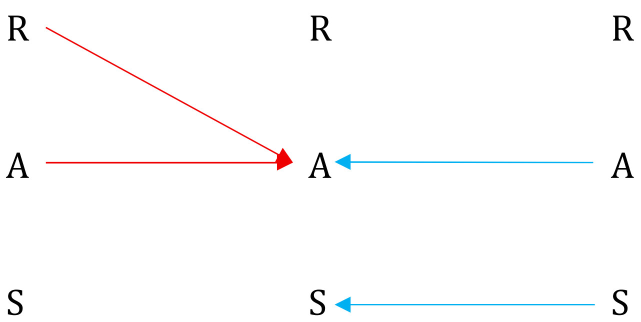



DS = [(R.A, A.S, S.R) × (R.S, S.A, A.R)]

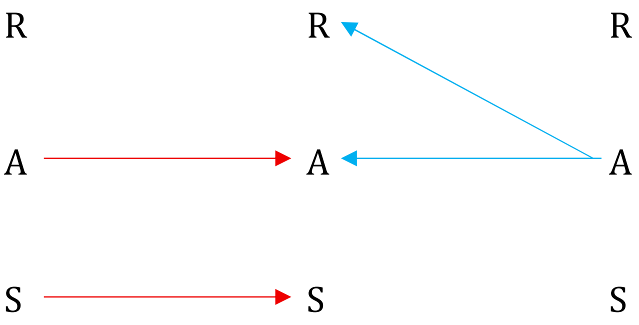



13. Raumsemiotische Relation

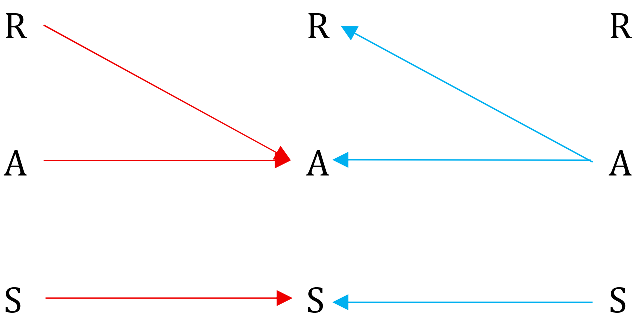
RR = (R.A, A.A, S.S)



DRR = (S.S, A.A, A.R)

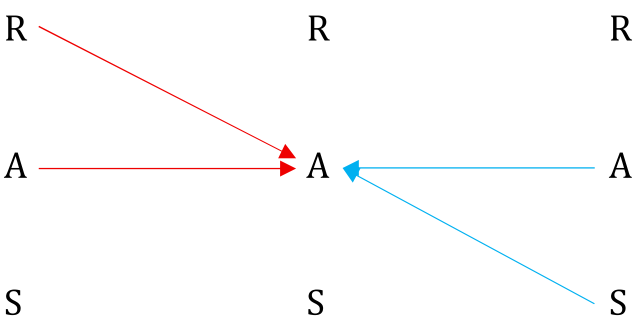



DS = [(R.A, A.A, S.S) × (S.S, A.A, A.R)]

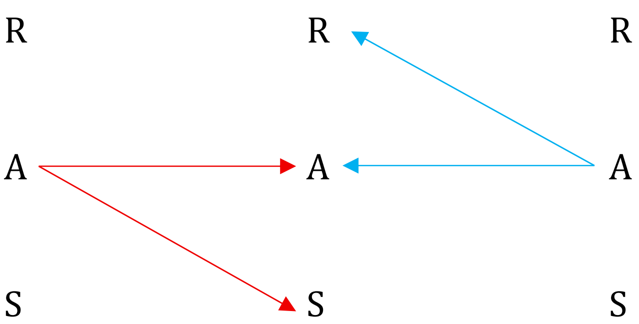



## 14. Raumsemiotische Relation

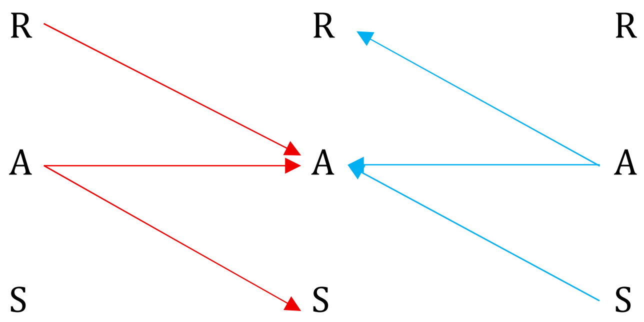
RR = (R.A, A.A, S.A)




DRR = (A.S, A.A, A.R)

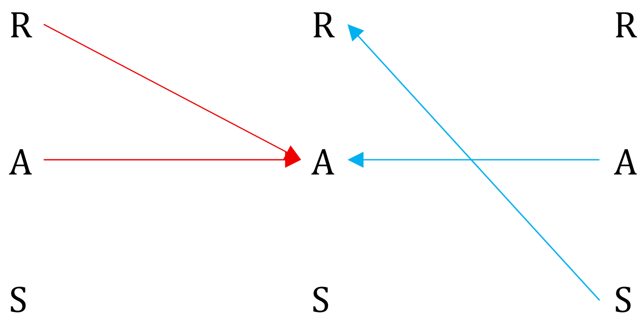


DS = [(R.A, A.A, S.A) × (A.S, A.A, A.R)]

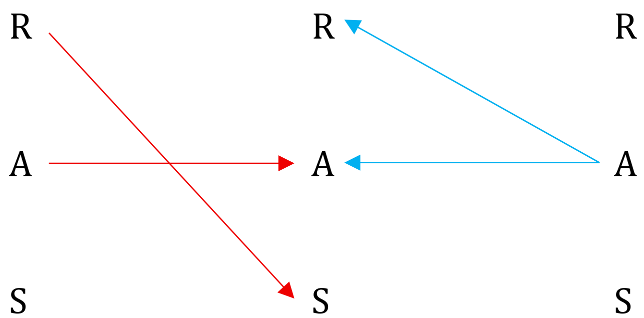



15. Raumsemiotische Relation

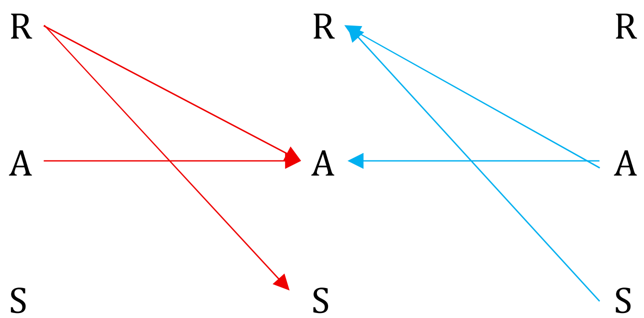
RR = (R.A, A.A, S.R)




DRR = (R.S, A.A, A.R)

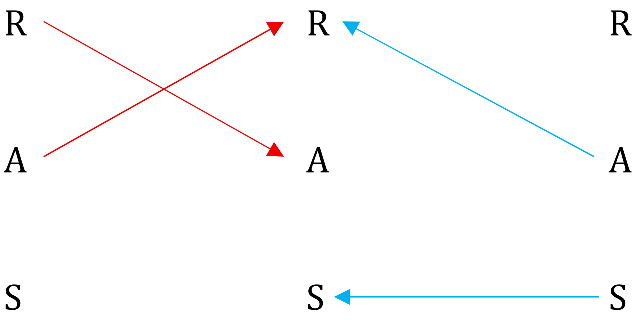



DS = [(R.A, A.A, S.R) × (R.S, A.A, A.R)]

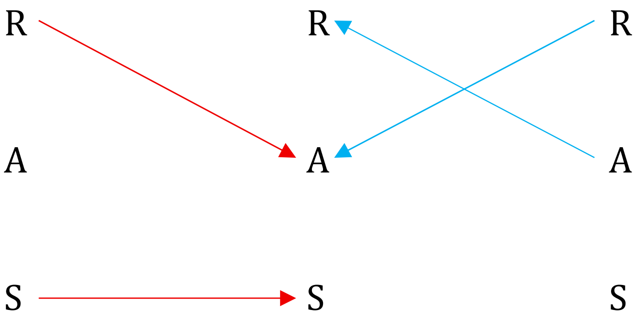


16. Raumsemiotische Relation

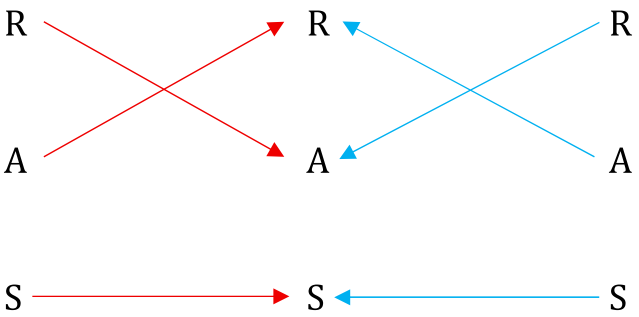
RR = (R.A, A.R, S.S)




DRR = (S.S, R.A, A.R)

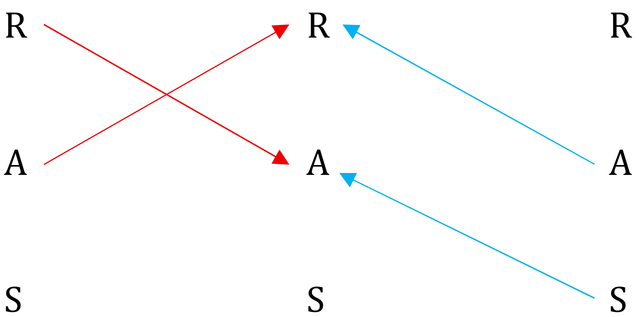



DS = [(R.A, A.R, S.S) × (S.S, R.A, A.R)]

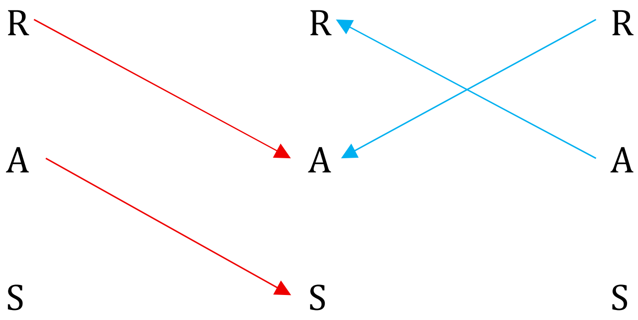



17. Raumsemiotische Relation

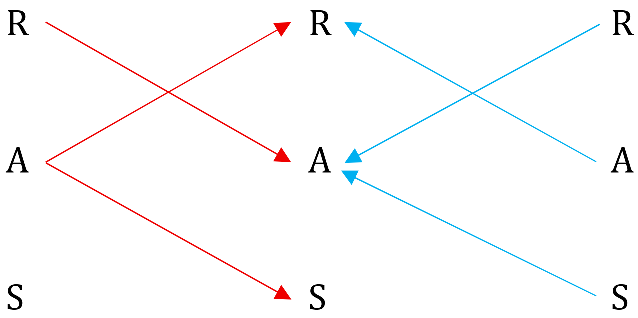
RR = (R.A, A.R, S.A)



DRR = (A.S, R.A, A.R)

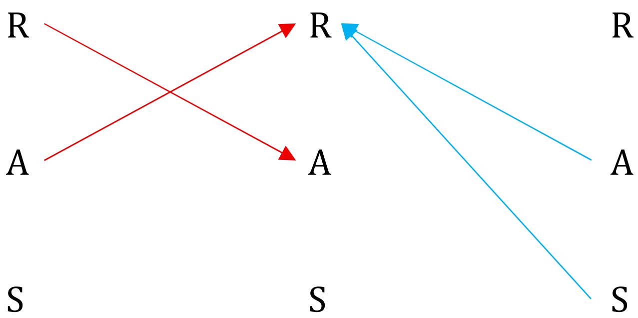



DS = [(R.A, A.R, S.A) × (A.S, R.A, A.R)]

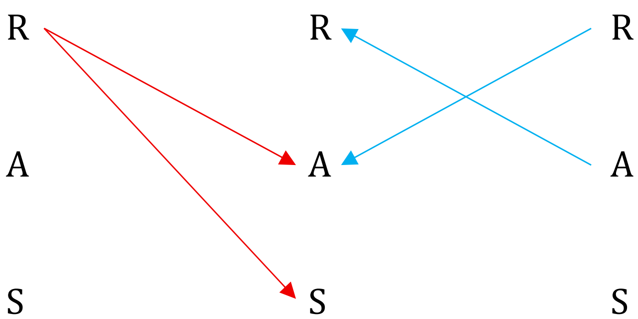



18. Raumsemiotische Relation

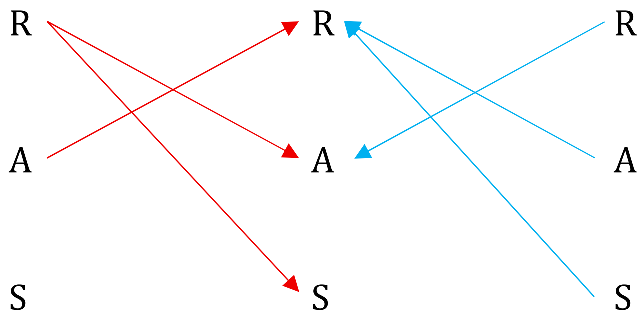
RR = (R.A, A.R, S.R)




DRR = (R.S, R.A, A.R)

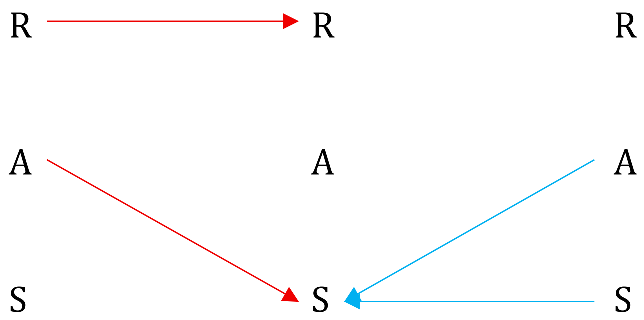


DS = [(R.A, A.R, S.R) × (R.S, R.A, A.R)]

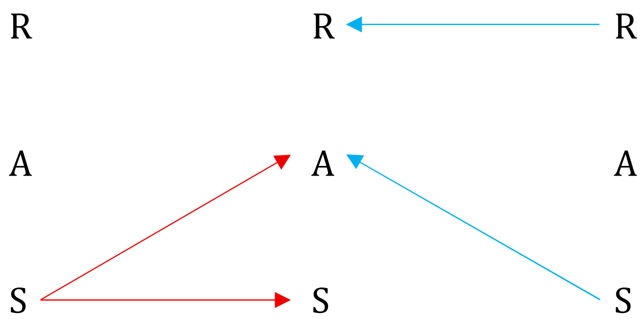



19. Raumsemiotische Relation

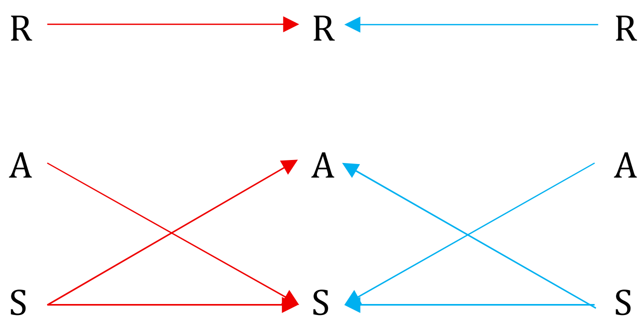
RR = (R.R, A.S, S.S)




DRR = (S.S, S.A, R.R)

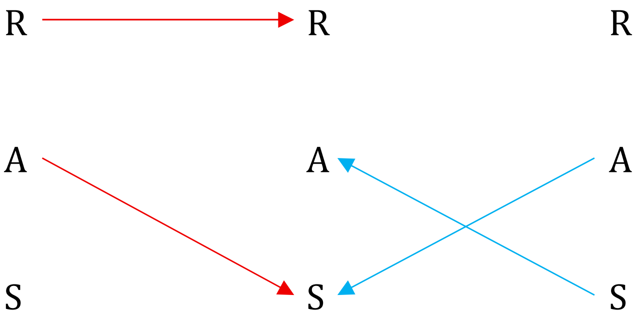



DS = [(R.R, A.S, S.S) × (S.S, S.A, R.R)]

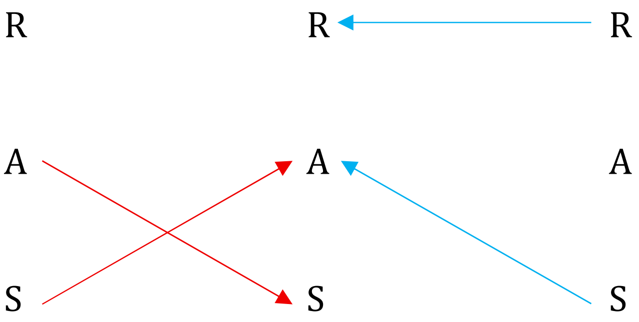


20. Raumsemiotische Relation

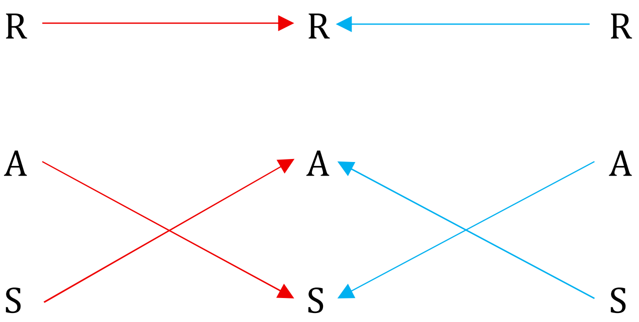
RR = (R.R, A.S, S.A)




DRR = (A.S, S.A, R.R)

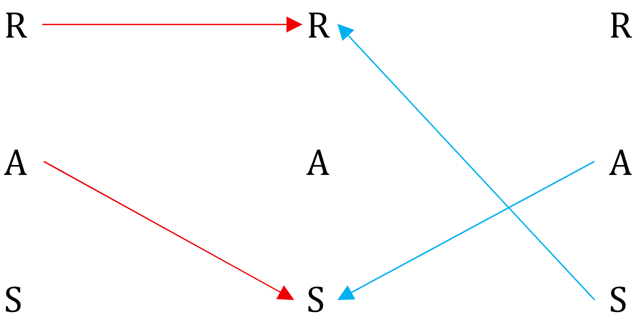



DS = [(R.R, A.S, S.A) × (A.S, S.A, R.R)]

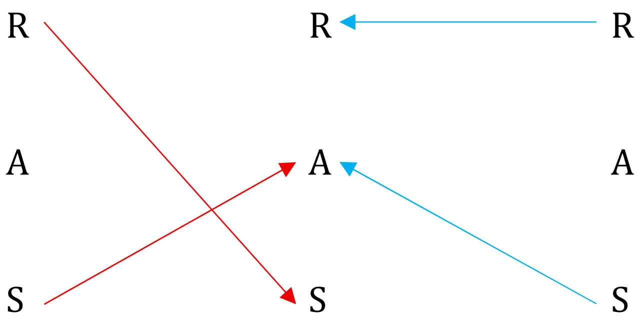



21. Raumsemiotische Relation

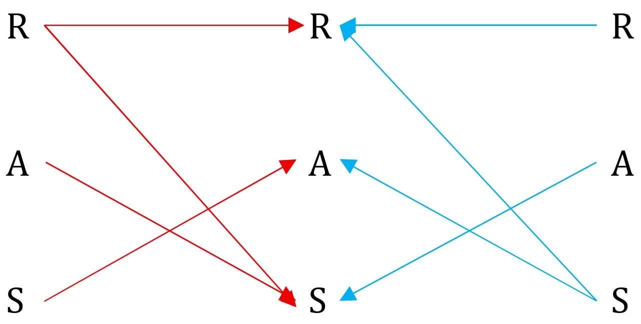
RR = (R.R, A.S, S.R)



DRR = (R.S, S.A, R.R)

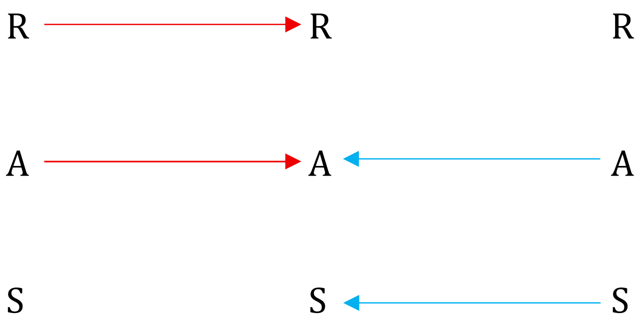



DS = [(R.R, A.S, S.R) × (R.S, S.A, R.R)]

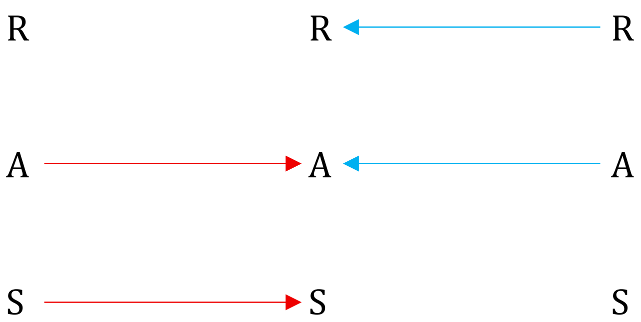



22. Raumsemiotische Relation

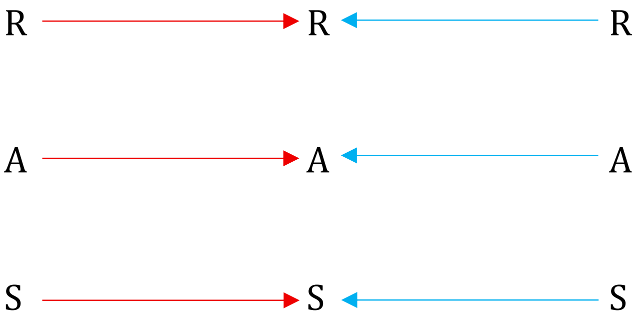
RR = (R.R, A.A, S.S)




DRR = (S.S, A.A, R.R)

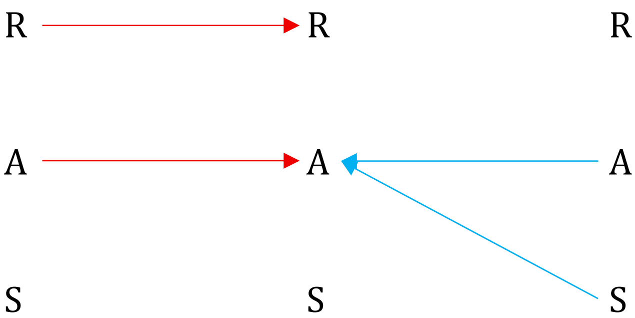


DS = [(R.R, A.A, S.S) × (S.S, A.A, R.R)]

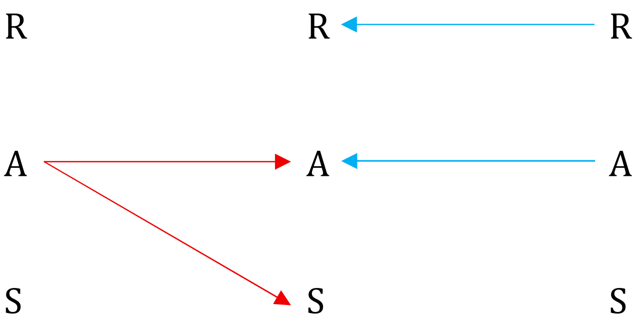



23. Raumsemiotische Relation

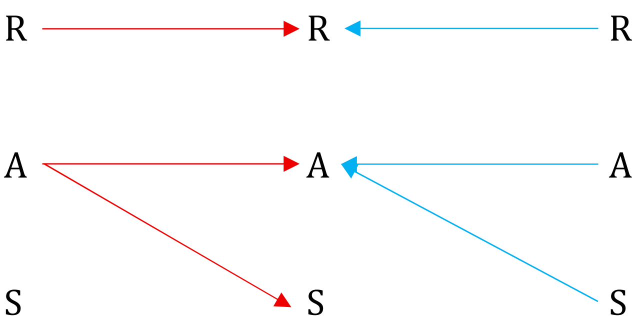
RR = (R.R, A.A, S.A)




DRR = (A.S, A.A, R.R)

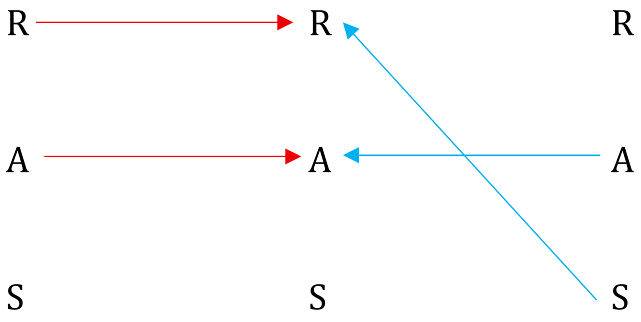



DS = [(R.R, A.A, S.A) × (A.S, A.A, R.R)]

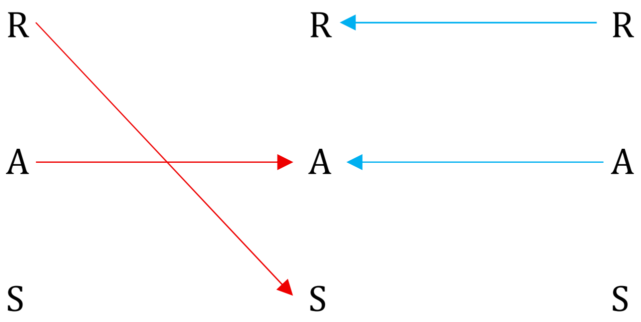


24. Raumsemiotische Relation

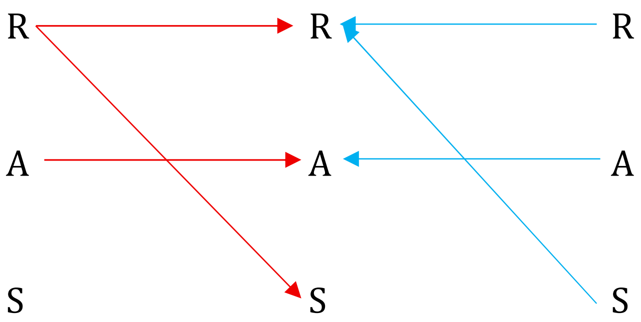
RR = (R.R, A.A, S.R)




DRR = (R.S, A.A, R.R)

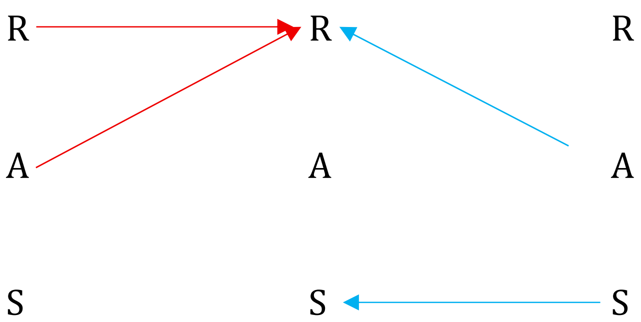



DS = [(R.R, A.A, S.R) × (R.S, A.A, R.R)]

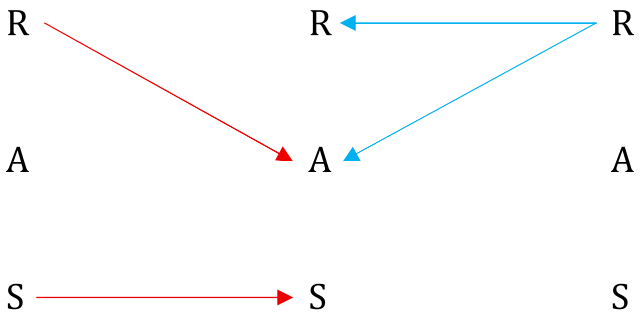



25. Raumsemiotische Relation

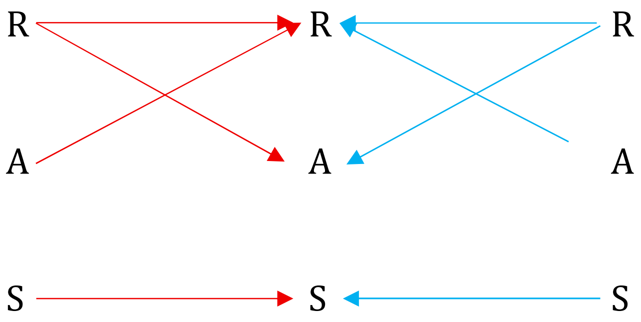
RR = (R.R, A.R, S.S)



DRR = (S.S, R.A, R.R)

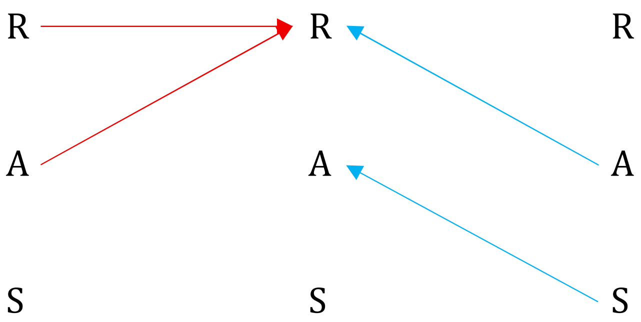



DS = [(R.R, A.R, S.S) × (S.S, R.A, R.R)]

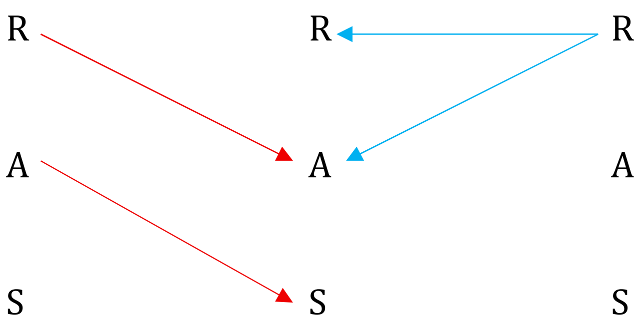



## 26. Raumsemiotische Relation

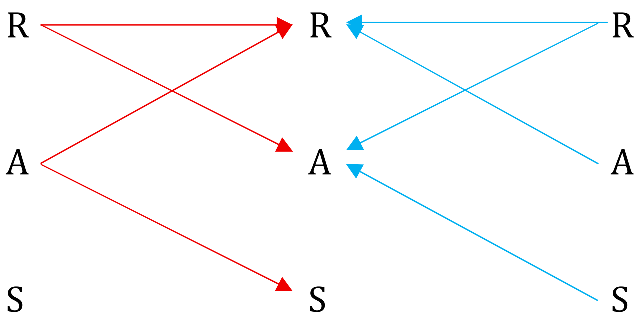
RR = (R.R, A.R, S.A)




DRR = (A.S, R.A, R.R)

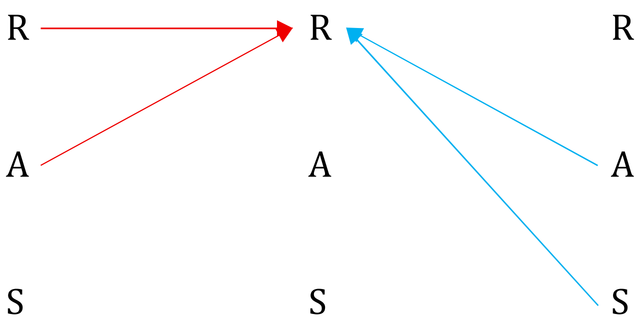


DS = [(R.R, A.R, S.A) × (A.S, R.A, R.R)]

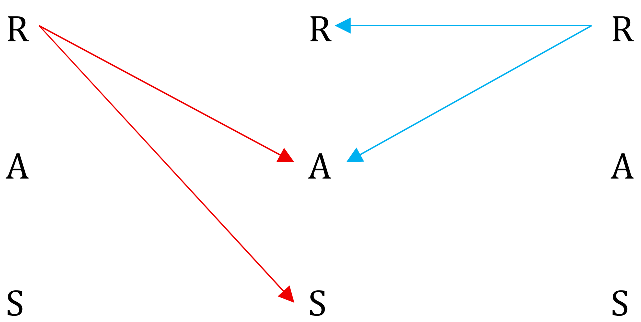



27. Raumsemiotische Relation

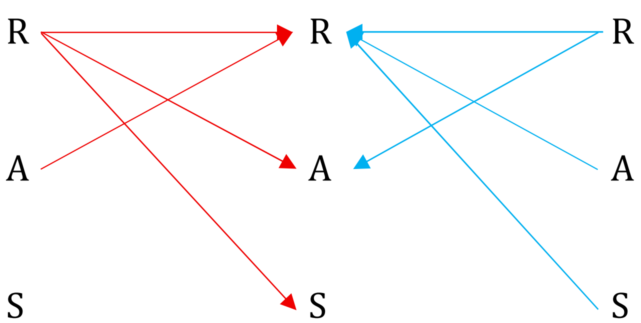
RR = (R.R, A.R, S.R)




DRR = (R.S, R.A, R.R)




DS = [(R.R, A.R, S.R) × (R.S, R.A, R.R)]

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